

# Appendix A: List of Symbols

$\%OS$	Percent overshoot
$A$	Ampere—unit of electrical current
$\mathbf{A}$	System matrix for state-space representation
$a_m$	Motor time constant
$B$	Mechanical rotational coefficient of viscous friction in N-m-s/rad
$\mathbf{B}$	Input matrix for state-space representation
$C$	Electrical capacitance in farads
$\mathbf{C}$	Output matrix for state-space representation
$C(s)$	Laplace transform of the output of a system
$c(t)$	Output of a system
$\mathbf{C_M}$	Controllability matrix
$D$	Mechanical rotational coefficient of viscous friction in N-m-s/rad
$\mathbf{D}$	Feedforward matrix for state-space representation
$D_a$	Motor armature coefficient of viscous damping in N-m-s/rad
$D_m$	Total coefficient of viscous friction at the armature of a motor, including armature coefficient of viscous friction and reflected load coefficient of viscous friction in N-m-s/rad
$E$	Energy
$E(s)$	Laplace transform of the error
$e(t)$	Error; electrical voltage
$E_a(s)$	Laplace transform of the motor armature input voltage; Laplace transform of the actuating signal
$e_a(t)$	Motor armature input voltage; actuating signal
$F$	Farad—unit of electrical capacitance
$F(s)$	Laplace transform of $f(t)$
$f(t)$	Mechanical force in newtons; general time function
$f_v$	Mechanical translational coefficient of viscous friction
$g$	Acceleration due to gravity
$G$	Electrical conductance in mhos
$G(s)$	Forward-path transfer function
$G_c(s)$	Compensator transfer function
$G_c(z)$	Sampled transfer function for a compensator
$G_M$	Gain margin
$G_p(z)$	Sampled transfer function for a plant

## Appendix A: List of Symbols

<b>H</b>	Henry—unit of electrical inductance
$H(s)$	Feedback-path transfer function
<b>I</b>	Identity matrix
$i(t)$	Electrical current in amperes
$J$	Moment of inertia in $\text{kg}\cdot\text{m}^2$
$J_a$	Motor armature moment of inertia in $\text{kg}\cdot\text{m}^2$
$J_m$	Total moment of inertia at the armature of a motor, including armature moment of inertia and reflected load moment of inertia in $\text{kg}\cdot\text{m}^2$
<b>K</b>	Controller gain matrix
$K$	Mechanical translational spring constant in N/m or rotational spring constant in N-m/rad; amplifier gain; residue
$k$	Controller feedback gain; running index
$K_a$	Acceleration constant
$K_b$	Back emf constant in V/rad/s
$K_f$	Feedback gain
kg	Kilogram = newton seconds <sup>2</sup> /meter—unit of mass
$\text{kg}\cdot\text{m}^2$	Kilogram meters <sup>2</sup> = newton-meters seconds <sup>2</sup> /radian—unit of moment of inertia
$K_m$	Motor gain
$K_p$	Position constant
$K_t$	Motor torque constant relating developed torque to armature current in N-m/A
$K_v$	Velocity constant
$L$	Electrical inductance in henries
<b>L</b>	Observer gain matrix
$l$	Observer feedback gain
$M$	Mass in kilograms; slope of the root locus asymptotes
$m$	Meter—unit of mechanical translational displacement
$M(\omega)$	Magnitude of a sinusoidal response
m/s	Meters/second—unit of mechanical translational velocity
$M_p$	Peak magnitude of the sinusoidal magnitude response
N	Newton—unit of mechanical translational force in kilogram meters/second <sup>2</sup>
N-s/m	Newton-seconds/meter—unit of mechanical translational coefficient of viscous friction
$n$	System type
N/m	Newton/meter—unit of mechanical translational spring constant
N-m	Newton-meter—unit of mechanical torque
N-m-s/rad	Newton-meter-seconds/radian—unit of mechanical rotational coefficient of viscous friction
N-m/A	Newton-meter/ampere—unit of motor torque constant
N-m/rad	Newton-meter/radian—unit of mechanical rotational spring constant
<b>O<sub>M</sub></b>	Observability matrix
<b>P</b>	Similarity transformation matrix
$p_c$	Compensator pole
Q	Coulomb—unit of electrical charge
$q(t)$	Electrical charge in coulombs

$R$	Electrical resistance in ohms
$R(s)$	Laplace transform of the input to a system
$r$	Nonlinear electrical resistance
$r(t)$	Input to a system
$R_a$	Motor armature resistance in ohms
rad	Radian—unit of angular displacement
rad/s	Radian/second—unit of angular velocity
s	Second—unit of time
$s$	Complex variable for the Laplace transform
$S_{F:P}$	Sensitivity of $F$ to a fractional change in $P$
$T$	Time constant; sampling interval for digital signals
$T(s)$	Closed-loop transfer function; Laplace transform of mechanical torque
$T(t)$	Mechanical torque in N-m
$T_m(t)$	Torque at the armature developed by a motor in N-m
$T_m(s)$	Laplace transform of the torque at the armature developed by a motor
$T_p$	Peak time in seconds
$T_r$	Rise time in seconds
$T_s$	Settling time in seconds
$T_w$	Pulse width in seconds
$\mathbf{u}$	Input or control vector for state-space representation
$u$	Input control signal for state-space representation
$u(t)$	Unit step input
V-s/rad	Volt-seconds/radian—unit of motor back emf constant
$v(t)$	Mechanical translation velocity in m/s; electrical voltage
$v_b(t)$	Motor back emf in volts
$v_e(t)$	Error voltage
$v_p(t)$	Power amplifier input in volts
$\mathbf{x}$	State vector for state-space representation
$x(t)$	Mechanical translation displacement in meters; a state variable
$\dot{x}$	Time derivative of a state variable
$\dot{\mathbf{x}}$	Time derivative of the state vector
$\mathbf{y}$	Output vector for state-space representation
$y(t)$	Output scalar for state-space representation
$z$	Complex variable for the z-transform
$z_c$	Compensator zero
$\alpha$	Pole-scaling factor for a lag compensator, where $\alpha > 1$ ; angle of attack
$\beta$	Pole-scaling factor for a lead compensator, where $\beta < 1$
$\gamma$	Pole-scaling factor for a lag-lead compensator, where $\gamma > 1$
$\delta$	Thrust angle
$\zeta$	Damping ratio
$\theta$	Angle of a vector with the positive extension of the real axis
$\theta(t)$	Angular displacement
$\theta_a$	Angle of a root locus asymptote with the positive extension of the real axis

$\theta_c$	Angular contribution of a compensator on the $s$ -plane
$\theta_m(t)$	Angular displacement of the armature of a motor
$\lambda$	Eigenvalue of a square matrix
$\sigma$	Real part of the Laplace transform variable, $s$
$\sigma_a$	Real-axis intercept of the root locus asymptotes
$\Phi_M$	Phase margin
$\Phi(t)$	State transition matrix
$\phi$	Sinusoidal phase angle; body angle
$\phi_c$	Sinusoidal phase angle of a compensator
$\phi_{max}$	Maximum sinusoidal phase angle
$\Omega$	Ohm—unit of electrical resistance
$\mathcal{U}$	Mho—unit of electrical conductance
$\omega$	Imaginary part of the Laplace transform variable, $s$
$\omega(t)$	Angular velocity in rad/s
$\omega_{BW}$	Bandwidth in rad/s
$\omega_d$	Damped frequency of oscillation in rad/s
$\omega_{\Phi_M}$	Phase-margin frequency in radians
$\omega_{G_M}$	Gain-margin frequency in radians
$\omega_n$	Natural frequency in rad/s
$\omega_p$	Peak-magnitude frequency of the magnitude frequency response in rad/s